

## U.G. 3rd Semester Examination - 2019

## PHYSICS

## [HONOURS]

Course Code : PHYS(H)CC-05-T

Full Marks : 40

Time :  $2\frac{1}{2}$  Hours*The figures in the right-hand margin indicate marks.**Candidates are required to give their answers in their own words as far as practicable.*

## GROUP-A

1. Answer any five questions:  $2 \times 5 = 10$ 

a) State Dirichlet's conditions for a Fourier series.

b) What do you mean by the orthogonality special functions?

c) Evaluate  $\Gamma\left(-\frac{1}{2}\right)$ .d) Prove the following property of the Beta function  $\beta(l, m) = \beta(m, l)$ .

e) What are the singular points of a second order linear differential equations?

f) What do you mean by random error?

[Turn over]

g) Write down the Parseval's formula.

b) Write down the relation between the Beta and Gamma function.

## GROUP-B

2. Answer any two questions:  $5 \times 2 = 10$ 

a) i) When does a Laguerre function transform to a Laguerre Polynomials? 2

ii) Find the constant  $a_0$  of the Fourier series for the function  $f(x) = x$  in  $0 \leq x \leq 2\pi$ . 3b) i) Evaluate  $\int_0^{\pi} \sqrt{x} e^{-\sqrt{x}} dx$ . 2

ii) Find the regular singular points of the differential equation

$$2x^2 \frac{d^2 y}{dx^2} + 3x \frac{dy}{dx} + (x^2 - 4)y = 0 \quad 3$$

c) Prove the orthogonality condition of Legendre Polynomials

$$\int_{-1}^1 P_m(x) P_n(x) dx = 0, \quad m \neq n \quad 5$$

- d) Write down the Bessel's differential equation of n-th order and its solution  $J_n(x)$ . 5

### GROUP-C

3. Answer any two questions: 10×2=20

- a) i) Find the Fourier series for the function  $f(x) = e^x$  for  $0 < x < \pi$ , where  $a$  is constant. 5

- ii) Find the integral  $\int_0^{\frac{\pi}{2}} \sin^m \theta \cos^n \theta d\theta$  using

$\beta(m, n)$  function in terms of  $\Gamma(x)$  function. 5

- b) Using Frobenius method, obtain a series solution in powers of  $x$  for differential equation:

$$2x(1-x)\frac{d^2y}{dx^2} + (1-x)\frac{dy}{dx} + 3y = 0 \text{ about } x=0.$$

10

- c) i) Find three dimensional Laplace's equation in cylindrical co-ordinates. 6

- ii) Prove that

$$\int_{-1}^{+1} P_n(x)(1-2xt+t^2)^{\frac{1}{2}} dx = \frac{2t^n}{2n+1}, \text{ given,}$$

$$\int_{-1}^{+1} [P_n(x)]^2 dx = \frac{2}{2n+1} \text{ where } n \text{ is a positive integer. 4.}$$

- d) A tightly stretched string with fixed end points at  $x=0$  and  $x=l$  is initially in a position given by

$$y = y_0 \sin^3\left(\frac{\pi x}{l}\right).$$

If it is released from rest from position  $x$  (within  $0 < x < l$ ), find the displacement  $y(x, t)$ . 10

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